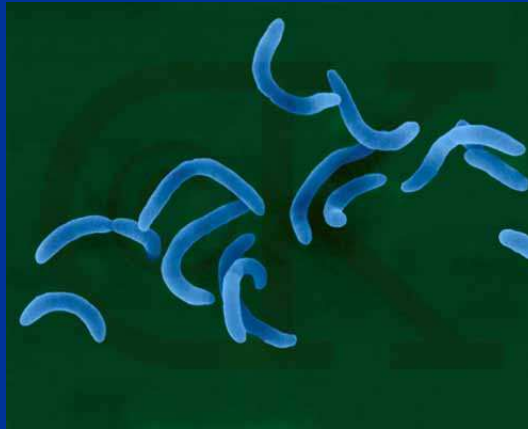


Basic rules of microbial growth

Fermentation up stream and down stream processes

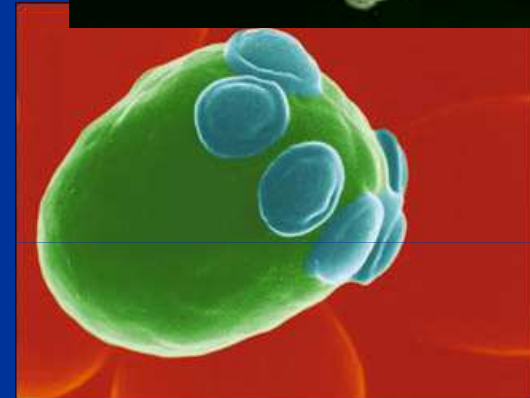


E.coli

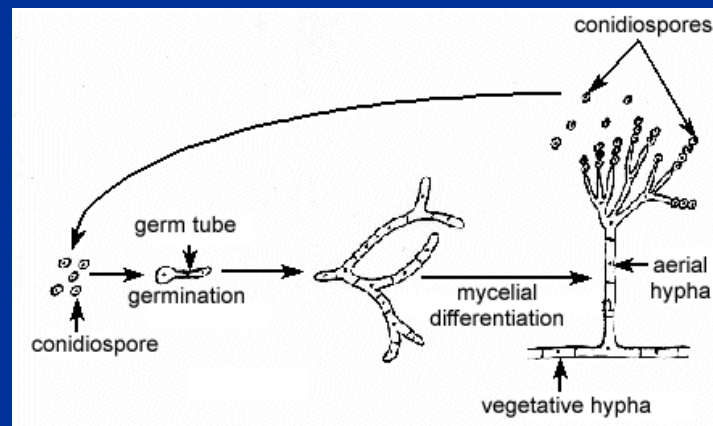


Vibrio cholerae

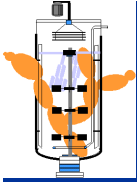
Saccharomyces cerevisiae



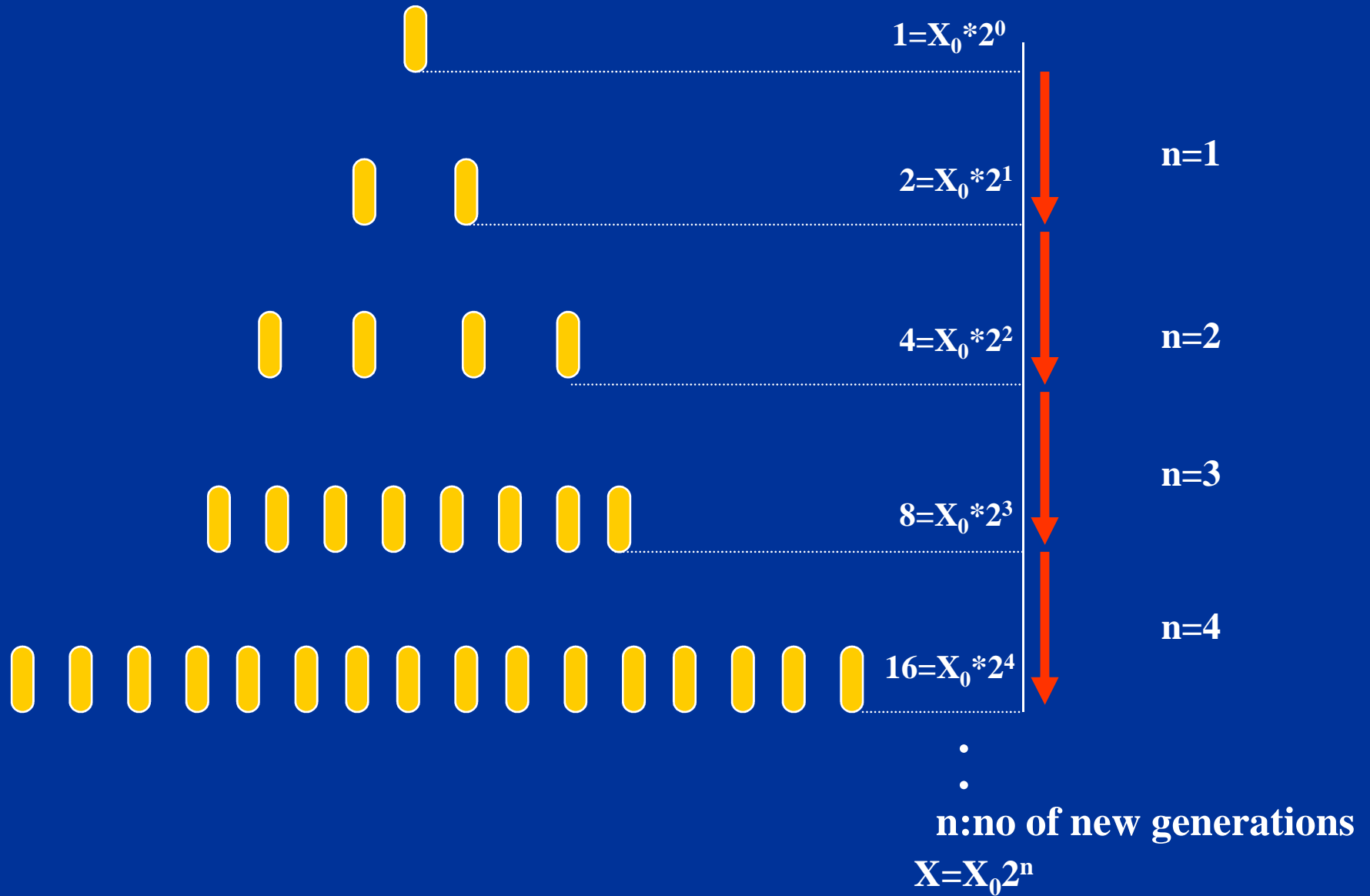
Mucor circinelloides



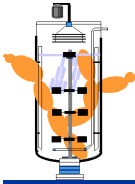
Aszexuális gombanövekedés



Basic rules of microbial growth



Binary dividing microorganisms



Basic rules of microbial growth

$$n = \frac{t}{t_g}$$

No of generations

Generációs idő - doubling time
generation time

Cell number pc/ml

N, x

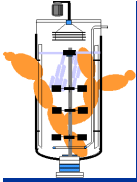
Cell mass: dw
mg/ml, g/l, kg/m³

$$X = X_0 2^{\frac{t}{t_g}} = X_0 2^n$$

MONOD, 1942

μ : specific growth rate

$$\frac{dx}{dt} = \mu \cdot X$$



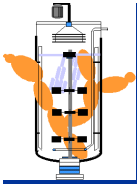
Basic rules of microbial growth

$$\frac{dx}{dt} = \mu \cdot x$$

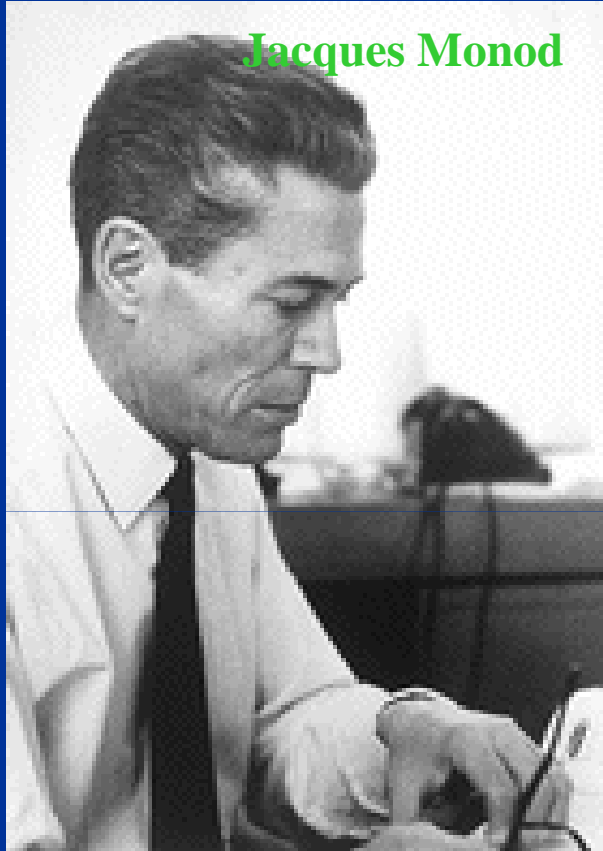
Specific growth rate

$$\mu \equiv \frac{1}{x} \frac{dx}{dt}$$

$$h^{-1}$$



Basic rules of microbial growth



Jacques Monod

$$\frac{dx}{dt} = \mu \cdot x$$



$$x = x_0 e^{\mu t}$$

Relation between μ and t_g :

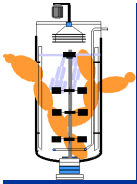
$$t_g = \frac{\ln 2}{\mu}$$

$$\frac{dN}{dt} = v \cdot N$$

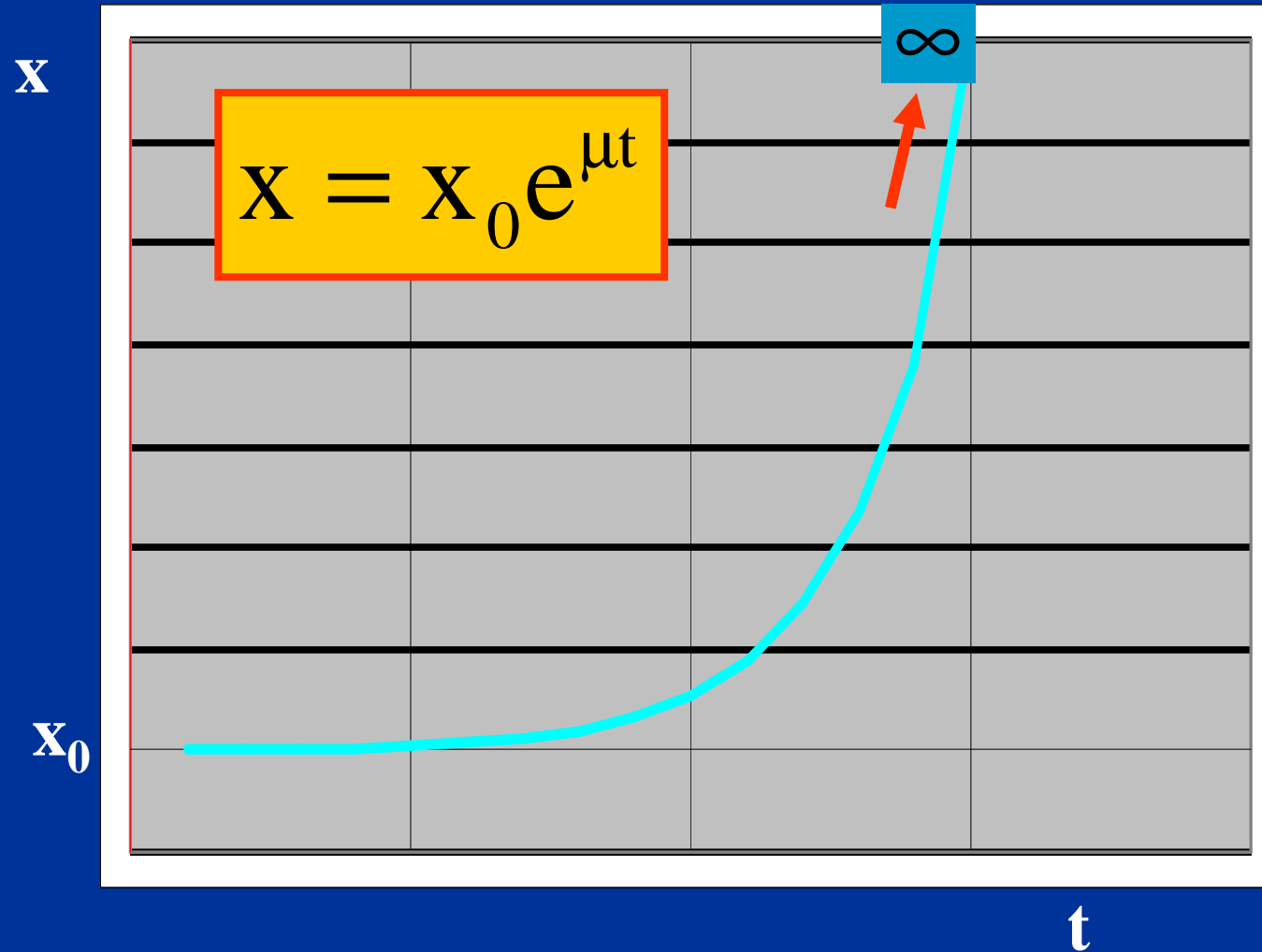


$$N = N_0 e^{vt}$$

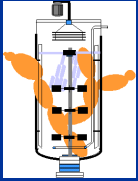
Specific proliferation rate
Spec. Doubling rate



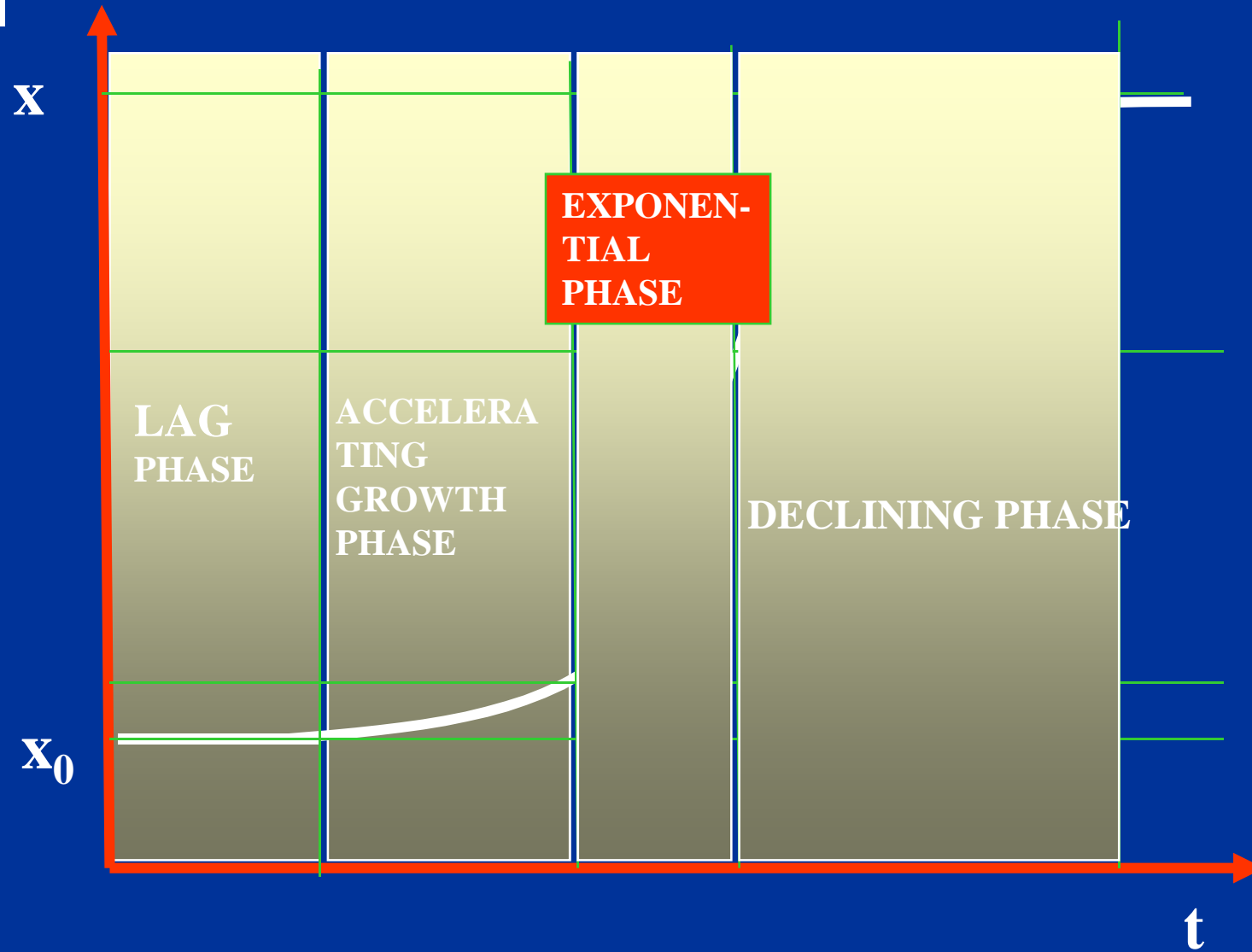
Basic rules of microbial growth

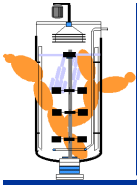


In reality

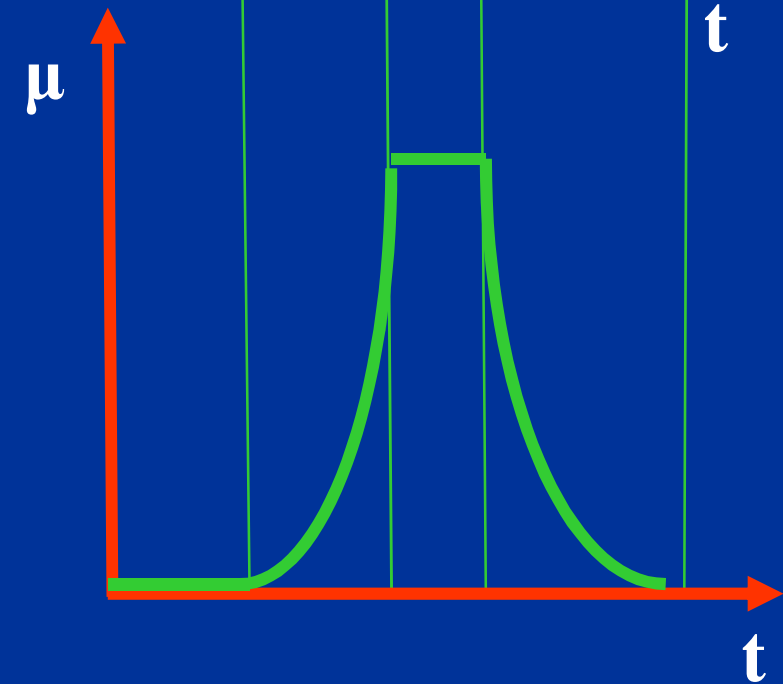
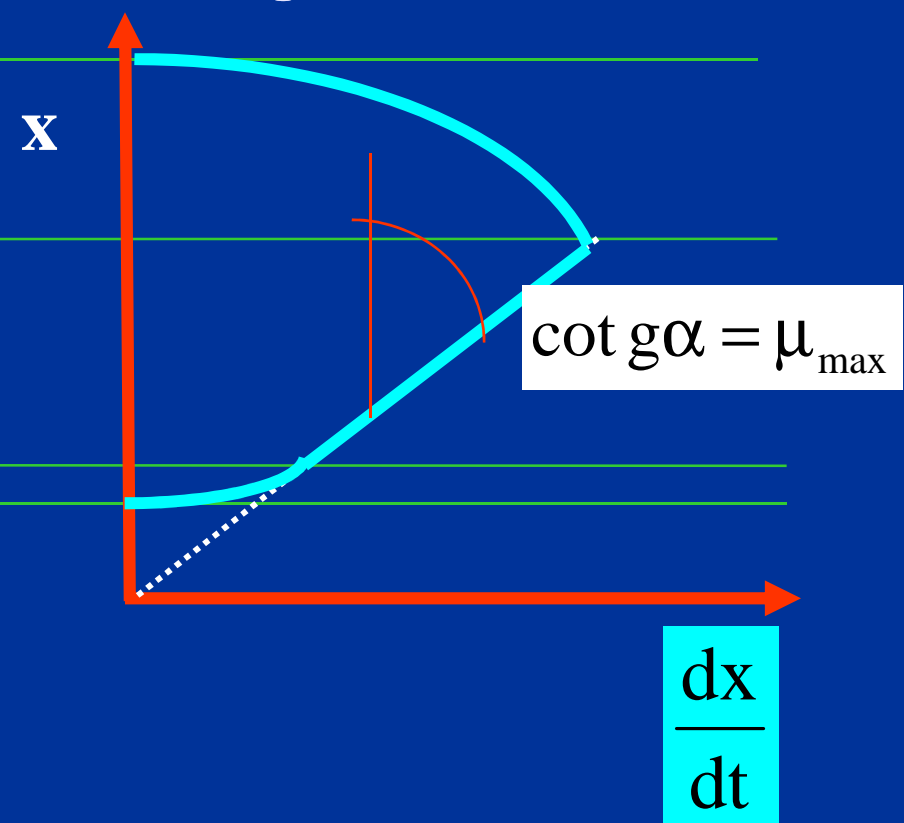
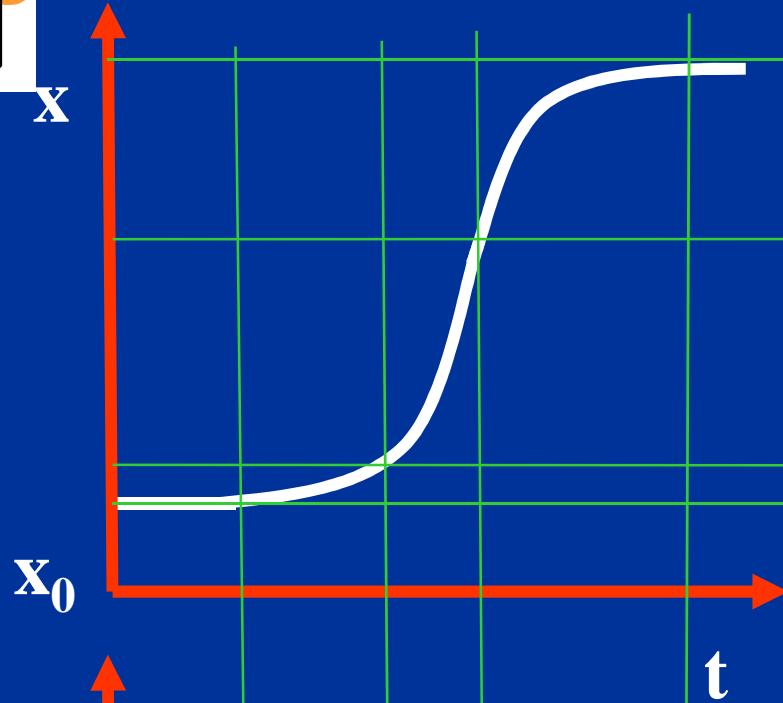


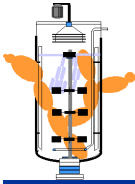
Basic rules of microbial growth





Basic rules of microbial growth





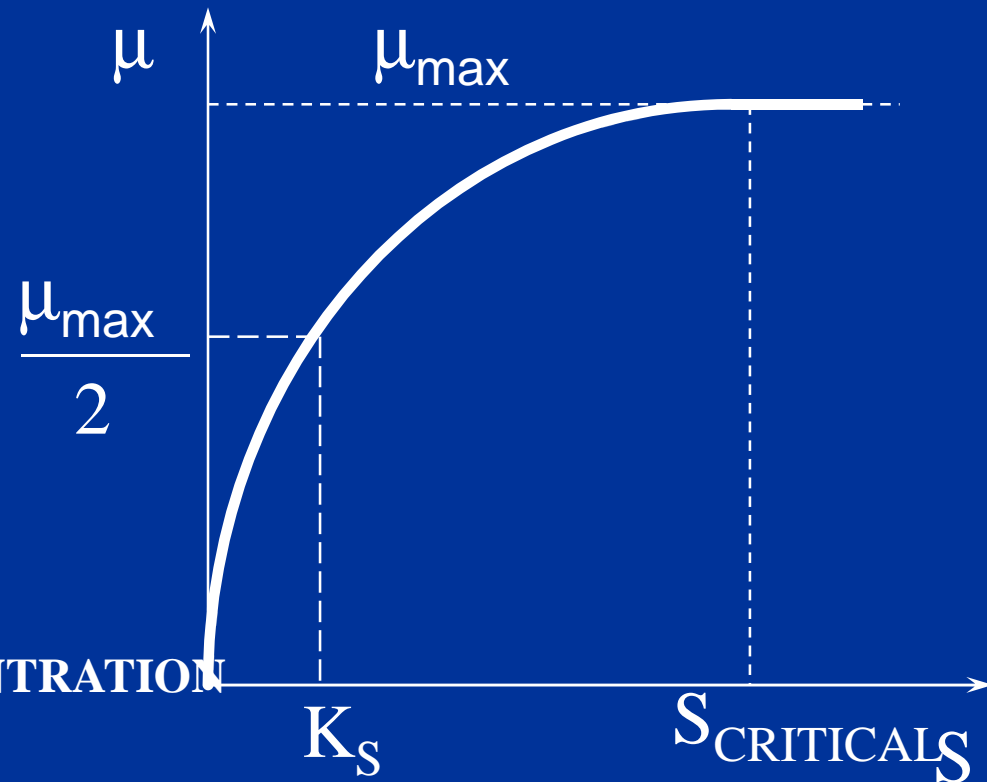
Basic rules of microbial growth

WHAT IS THE REASON OF THE EXISTENCE OF DECLINING PHASE?

1. NUTRIENT LIMITATION
2. TOXIC METABOLITE PRODUCT(S)
3. LACK OF SPACE

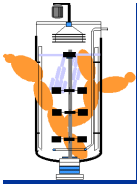
MONOD- model

$$\mu = \mu_{\max} \frac{S}{K_S + S}$$



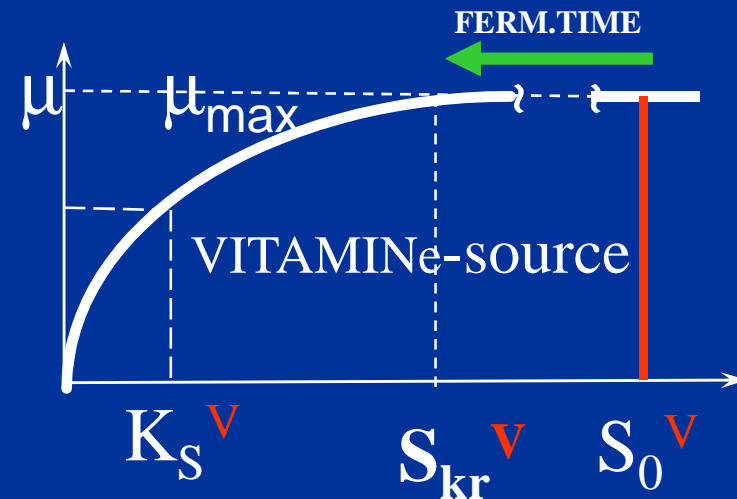
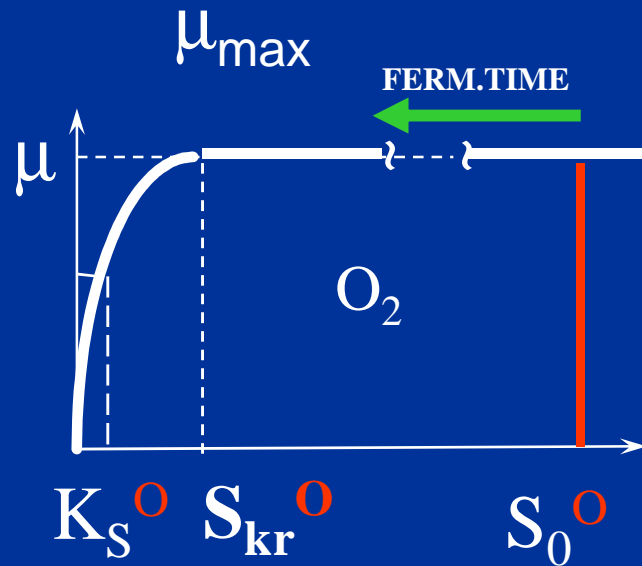
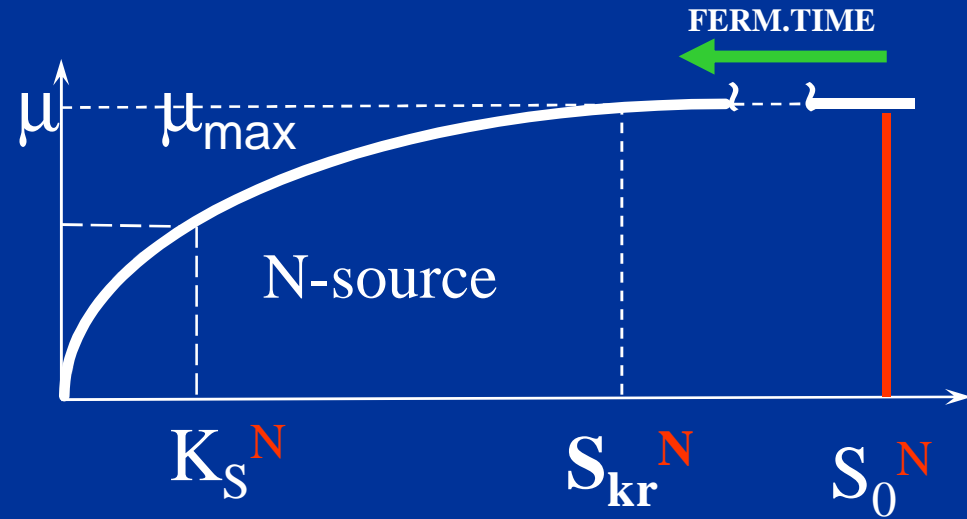
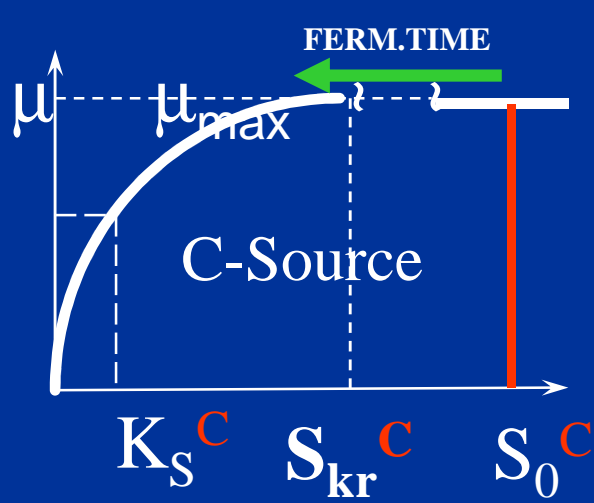
KRITICAL SUBSTRATE CONCENTRATION

LIMITING SUBSTRATE

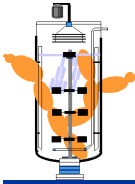


Basic rules of microbial growth

WHICH S WILL BE LIMITING ???

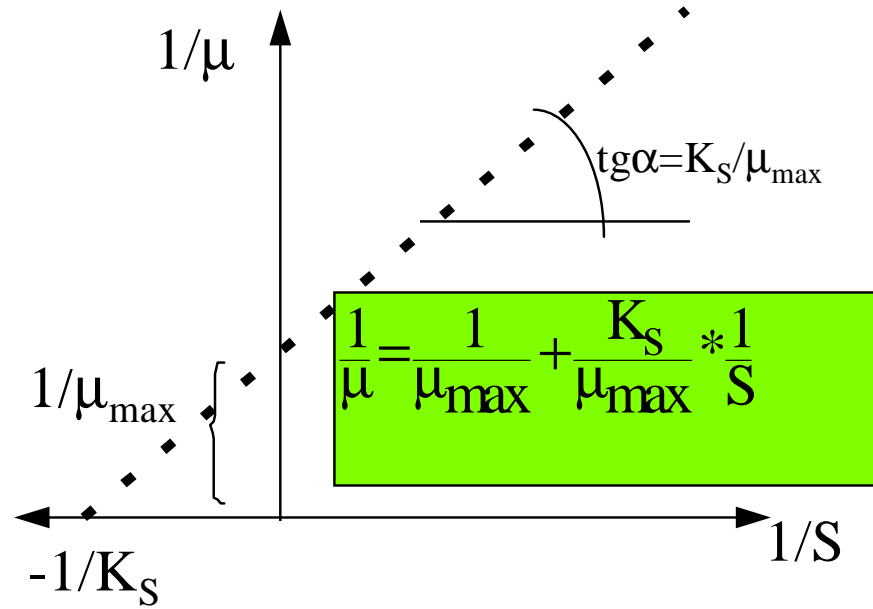


NOTION OF THE LIMITING SUBSTRATE

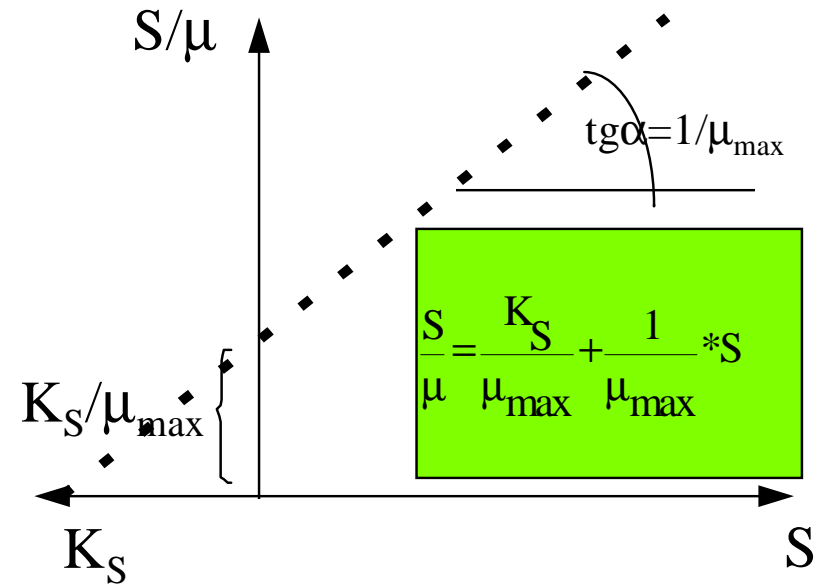


Basic rules of microbial growth

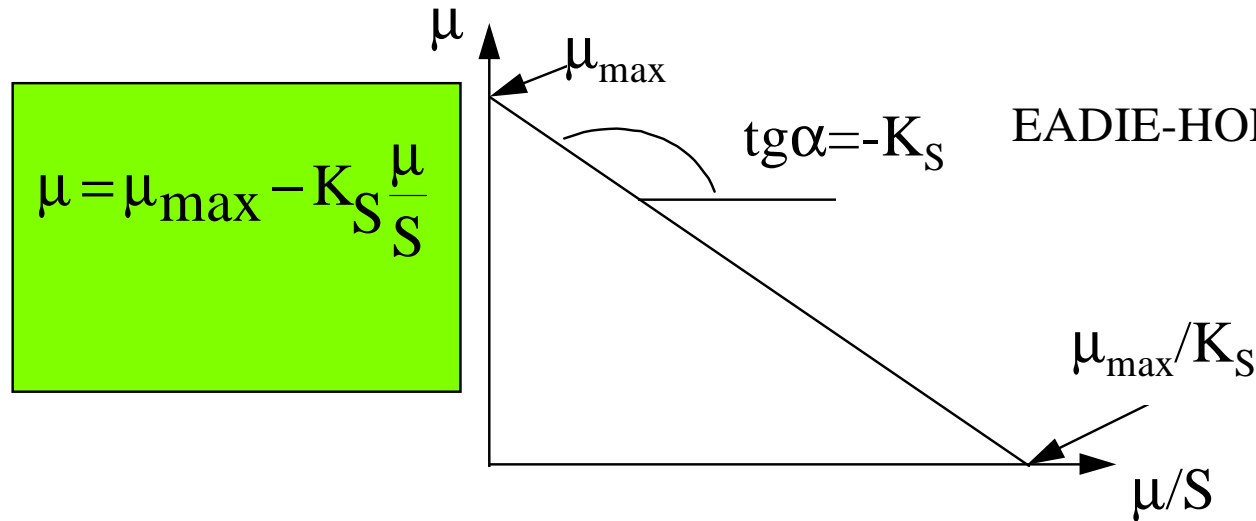
LINEWEAVER-BURK

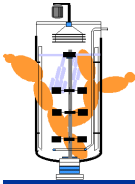


HANES v. LANGMUIR



EADIE-HOFSTEE





Basic rules of microbial growth

FOR THE LIMITING S

YIELD COEFF:

$$\frac{dx}{dS} = -Y_{x/s} = \frac{\Delta x}{\Delta S} = \frac{\frac{1}{x} \frac{dx}{dt}}{\frac{1}{S} \frac{dS}{dt}}$$

EXTENSION

$$\frac{dx}{dS_i} = -Y_{x/s_i} \quad \text{vagy} \quad -Y_i$$

ALWAYS TRUE:

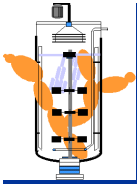
$$r_x = \frac{dx}{dt} = \mu x$$

In the exponential and declining phase:

$$r_x = \frac{dx}{dt} = \mu \frac{S}{K_s + S} x$$
$$r_s = \frac{dS}{dt} = -\frac{1}{Y_{x/S}} \mu \frac{S}{K_s + S} x$$

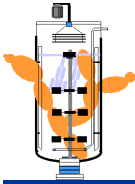
Differential equation
Can be solved

MONOD-model



Basic rules of microbial growth

$$\frac{dx}{dS_i} = \frac{\Delta x}{\Delta S} = \frac{\frac{dx}{dt}}{\frac{dS}{dt}} = \frac{\mu_x}{\mu_s} = \frac{\mu_x}{Q_s} - Y_{x/s_i} \quad \text{vagy} = -Y_i$$



Basic rules of microbial growth

Utilization of C/en source

What for?

incorporation energy production

$$\Delta S = \Delta S_C + \Delta S_E$$

$$\frac{\Delta S}{\Delta X} = \frac{\Delta S_C}{\Delta X} + \frac{\Delta S_E}{\Delta X}$$

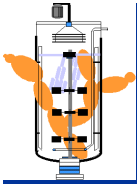
$$\frac{1}{Y_{x/s}} = \frac{1}{Y_C} + \frac{1}{Y_E}$$

$$Y_E = \frac{1}{\frac{1}{Y} - \frac{1}{Y_C}} = \frac{YY_C}{Y_C - Y}$$

Overall yield

Yield of incorp. carbon

Energy yield



Basic rules of microbial growth

Material balance for the incorporated carbon

$$\alpha_2 \Delta X = \alpha_1 \Delta S_C$$

C-content of the cell mass

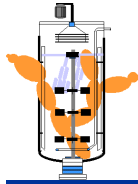
0,46-0,5 50%

C-content of the substrate

Glucose:0,4

$$\frac{\Delta X}{\Delta S_C} = Y_C = \frac{\alpha_1}{\alpha_2}$$

$$Y_E = \frac{Y \cdot \frac{\alpha_1}{\alpha_2}}{\frac{\alpha_1}{\alpha_2} - Y} = \frac{Y \cdot \alpha_1}{\alpha_1 - Y \cdot \alpha_2}$$



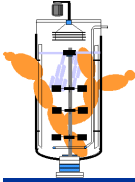
Basic rules of microbial growth

Some cases from the product one can estimate the energy production and consumption

EtOH	yeast, sugar	
AcOH	<i>A.aceti</i> , alcohol	NADH !!!
Glükonsav	<i>A.suboxydans</i> , glucose	

Strain	cult. media	Assimilated	Dissimilated
		ratio of cult. media %	ratio of cult. media %
<i>Streptococcus faecalis</i> anaerobic growth	complett	2	98
<i>Saccharomyces cerevisiae</i> aerobic growth	complett	10	90
<i>Saccharomyces cerevisiae</i> anaerobic growth	complett	2	98
<i>Aerobacter cloaceae</i> minimal	minimal	55	45

1,2,3,



Basic rules of microbial growth

$$\Delta S = \Delta S_c + \Delta S_E$$



?

Cell growth

Maintenance of viability

Cell motion

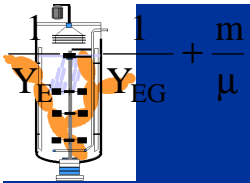
Osmotic work

Maintenance of orderness

thermodynamics II.law

resyntheses

$$Y_E = \frac{\Delta x}{\Delta S_E} = \frac{\Delta x}{\Delta S_g + \Delta S_m}$$



Basic rules of microbial growth

$$\frac{dS}{dt} = -\frac{1}{Y} \frac{dx}{dt} = -\frac{\mu x}{Y}$$

!!!

$$\left(\frac{dS}{dt}\right)_E = \frac{\mu_x}{Y_E} = \frac{dS_g}{dt} + \frac{dS_m}{dt}$$

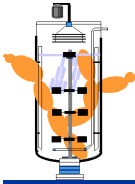
$$\frac{dS_g}{dt} = \frac{\mu x}{Y_{EG}}$$

$$\frac{dS_m}{dt} = m x$$

modell

$$\frac{\mu x}{Y_E} = \frac{\mu x}{Y_{EG}} + m x$$

$$\frac{1}{Y_E} = \frac{1}{Y_{EG}} + \frac{m}{\mu}$$



Basic rules of microbial growth

$$\frac{1}{Y_E} = \frac{1}{Y_{EG}} + \frac{m}{\mu}$$

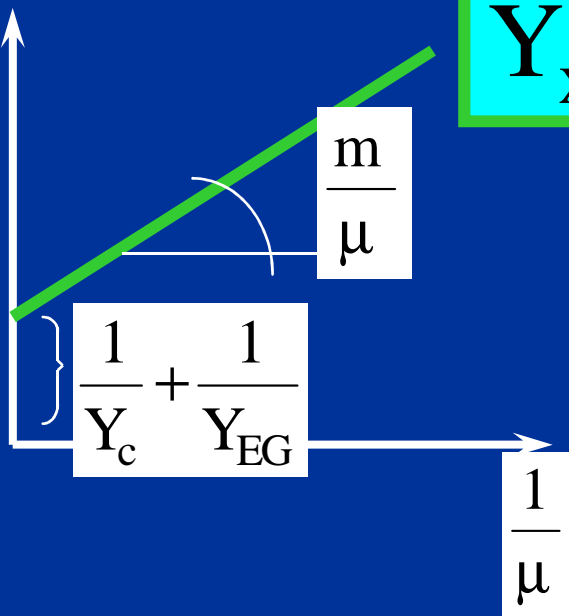
specific maintenance coefficient

$g/gh = h^{-1}$

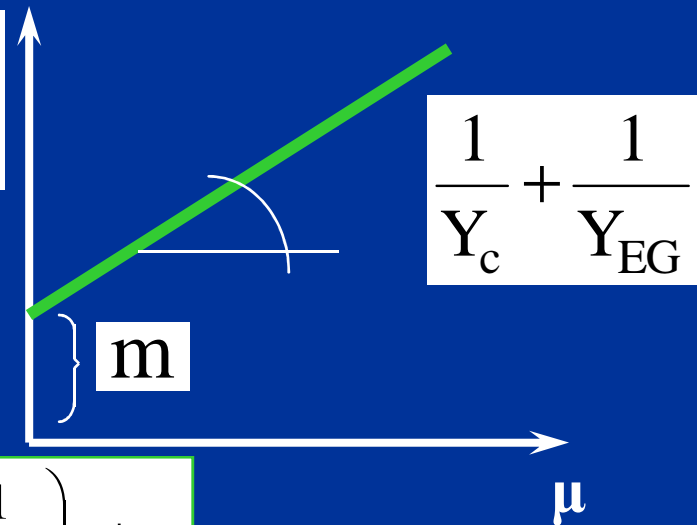
For the overall yield:

$$\frac{1}{Y_{x/s}} = \frac{1}{Y_c} + \frac{1}{Y_{EG}} + \frac{m}{\mu}$$

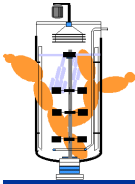
$$\frac{1}{Y_{x/s}}$$



$$\frac{\mu}{Y_{x/s}} = \mu_s$$



$$\mu_s = \left(\frac{1}{Y_c} + \frac{1}{Y_{EG}} \right) \mu + m$$



Basic rules of microbial growth

ATP-yield

$$Y_{\text{ATP}} = \frac{\Delta x}{\Delta \text{ATP}} = \frac{Y'_{x/s}}{Y_{\text{ATP}/s}}$$

g/mol

g/mol

mol/mol

$$Y'_{x/s} = M Y_{x/s}$$

10,5 g/mol

(8,3-32)

$$\Delta \text{ATP} = (\Delta \text{ATP})_g + (\Delta \text{ATP})_m$$

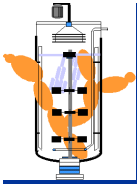
$$\frac{1}{Y_{\text{ATP}}} = \frac{1}{Y_{\text{ATP}}^{\text{max}}} + \frac{m_{\text{ATP}}}{\mu}$$

$$Q_{\text{ATP}} = \frac{\mu}{Y_{\text{ATP}}} = \frac{\mu}{Y_{\text{ATP}}^{\text{max}}} + m_{\text{ATP}}$$

**culture
conditions**

**specific mentenance
coefficients**

		m	m_{ATP}
<i>Aerobacter cloaceae</i>	aerobic, glucose	0,094	14
<i>Saccharomyces cerevisiae</i>	anaerobic glucose + 0,1 mol/dm ³ NaCl	0,036	0,52
<i>Saccharomyces cerevisiae</i>	anaerobic, glucose +1,0 mol/dm ³ NaCl	0,360	2,2
<i>Penicillium chrysogenum</i>	aerobic	0,022	3,2
<i>Lactobacillus casei</i>	aerobic, glucose	0,135	1,5



Basic rules of microbial growth

$$\frac{P}{O}$$

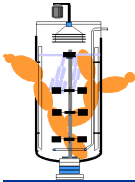
Effectivity of oxidative phosphorylation

mol/gatom

„P/O ratio”



$$Y_{\frac{p}{s}} = \frac{\Delta P}{\Delta S} \quad Y_{\frac{p}{x}} = \frac{\Delta P}{\Delta X}$$



Basic rules of microbial growth

METABOLIC
HEAT PRODUCTION

$$Y_H = Y_{\text{kcal}} = \frac{\Delta x}{-\Delta H_x \cdot \Delta x + \Delta H_s \cdot \Delta S} = \frac{\Delta x}{\Delta Q}$$

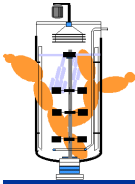
HEAT PROD. YIELD

ENTHALPY OF
CELL MASS

ENTHALPY OF SUBSTRATE

$$Y_H = Y_{\text{kcal}} = \frac{\Delta x / \Delta S}{-\Delta H_x \cdot \Delta x / \Delta S + \Delta H_s \cdot \Delta S / \Delta S} = \frac{Y_{x/S}}{\Delta H_s - Y_{x/S} \Delta H_x}$$

IF THERE IS NO SIGNIFICANT EXTRACELLULAR PRODUCTION



Basic rules of microbial growth

RQ respiration quotient

$$\frac{\frac{\Delta \text{CO}_2}{\Delta \text{O}_2}}{\frac{d\text{CO}_2}{d\text{O}_2}} = \frac{\frac{d\text{CO}_2}{dt}}{\frac{d\text{O}_2}{dt}} = \frac{q_{\text{CO}_2}}{q_{\text{O}_2}}$$



$$\text{RQ}_{\text{max}} = 1$$



$$\text{RQ}_{\text{max}} = 4/6 = 0,67$$



$$\text{RQ}_{\text{max}} = \infty$$



$$\text{RQ}_{\text{max}} = 2/3 = 0,67$$



$$\text{RQ}_{\text{max}} = 2 / \frac{1}{2} = 4$$

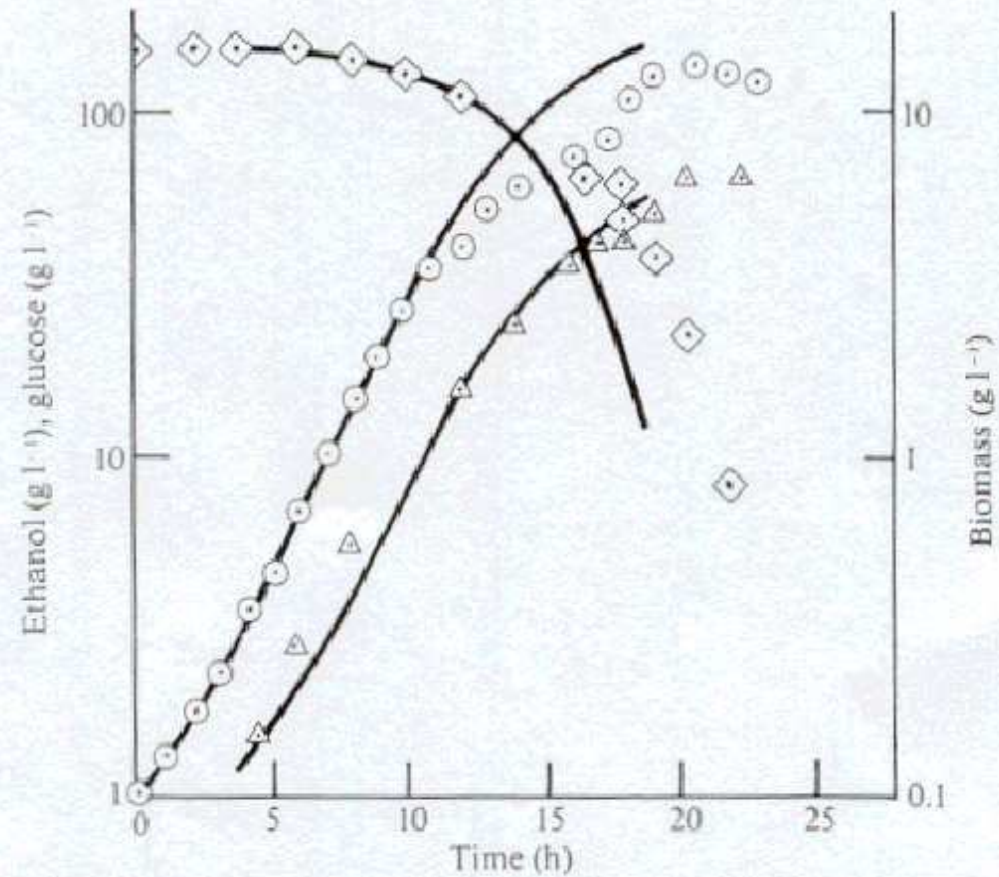
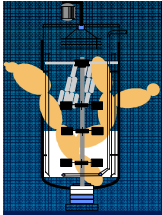


Fig. 6.59. Batch ethanol fermentation by *Saccharomyces cerevisiae*. Observed values; \odot , biomass; \triangle , ethanol; \diamond , glucose (Aiba et al., 1968).

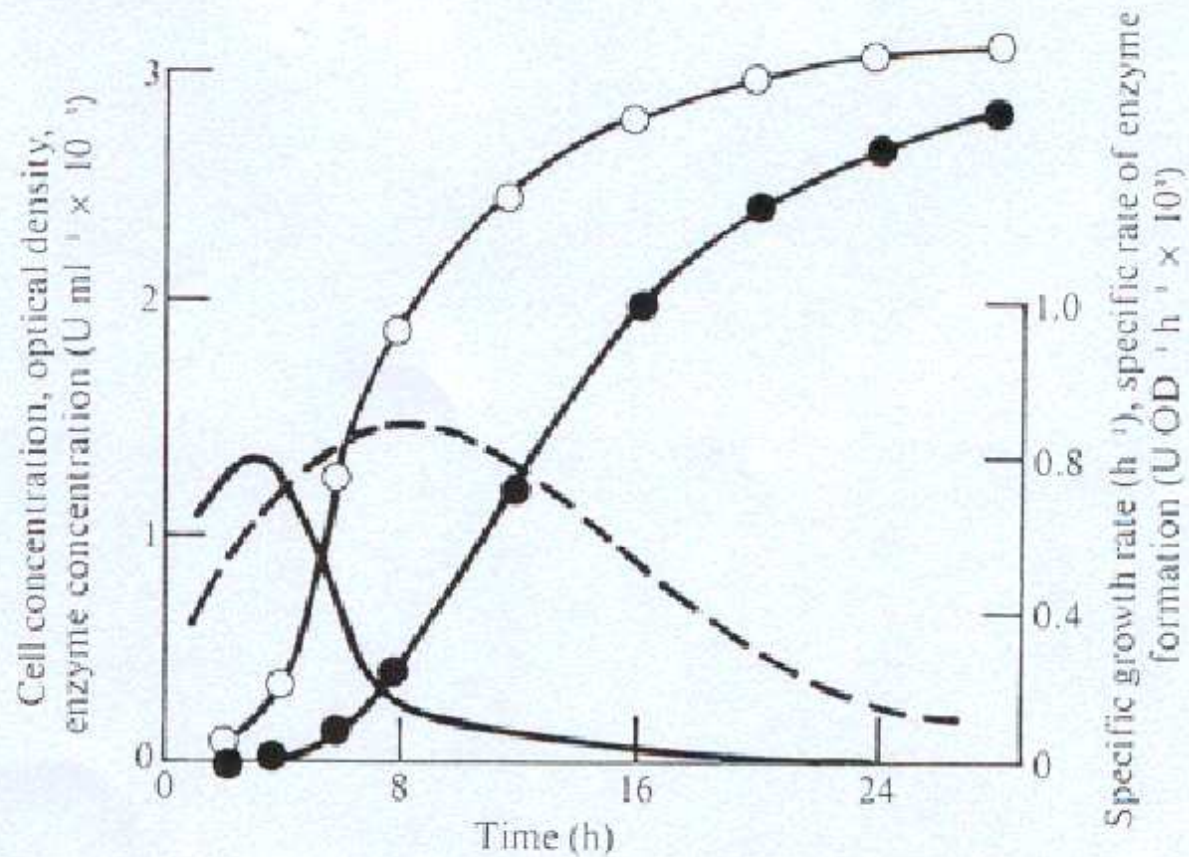
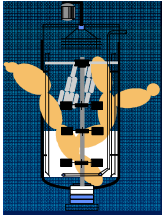
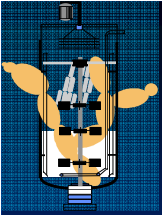
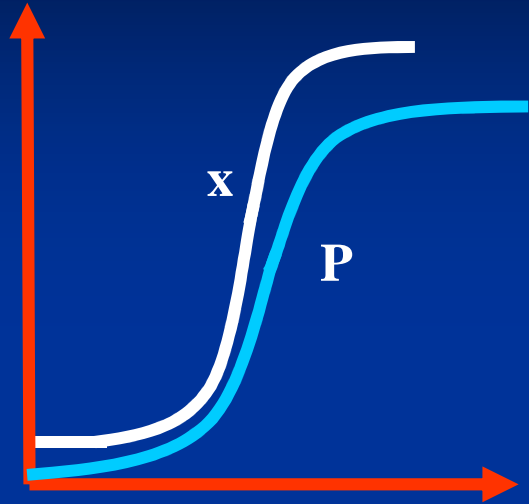


Fig. 6.53. Time course of α -amylase formation by *Bacillus amyloliquefaciens*. —, specific growth rate (μ); , specific rate of enzyme formation (ϵ); —○—, cell concentration (x); —●—, enzyme concentration (E).



GAEDEN: production types

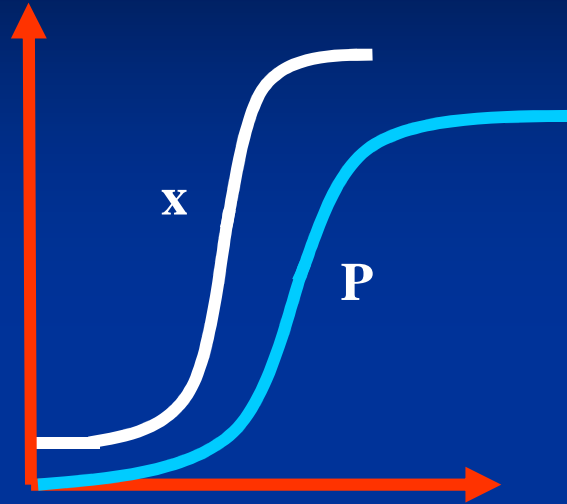
Primary products



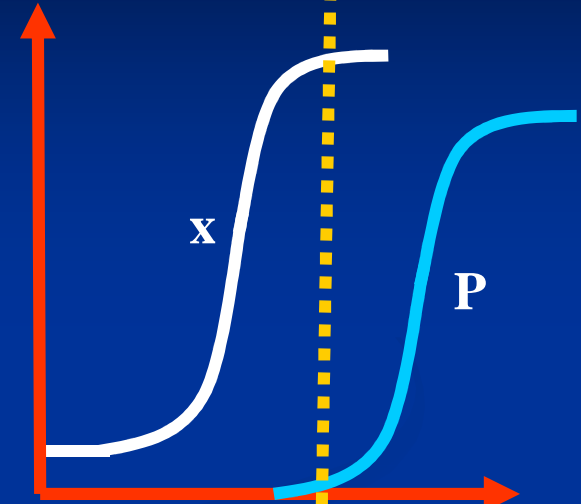
Growth associated

.....

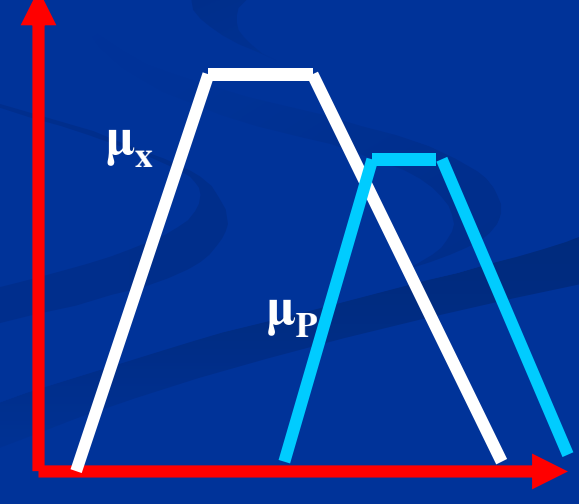
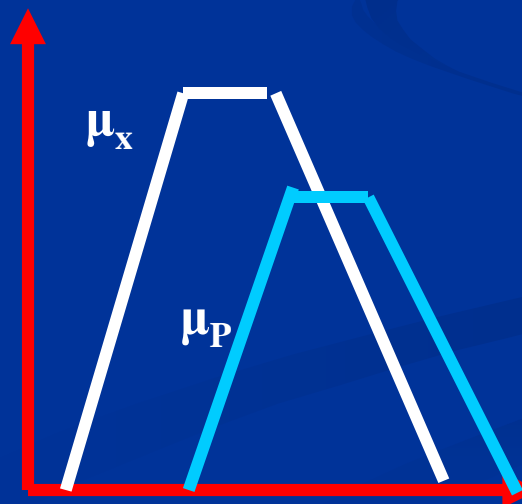
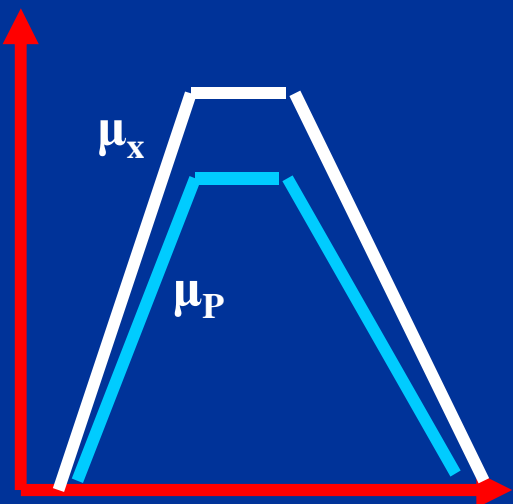
Secondary products

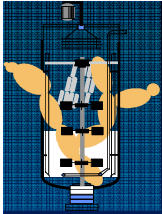


Mixed type



Non growth associated



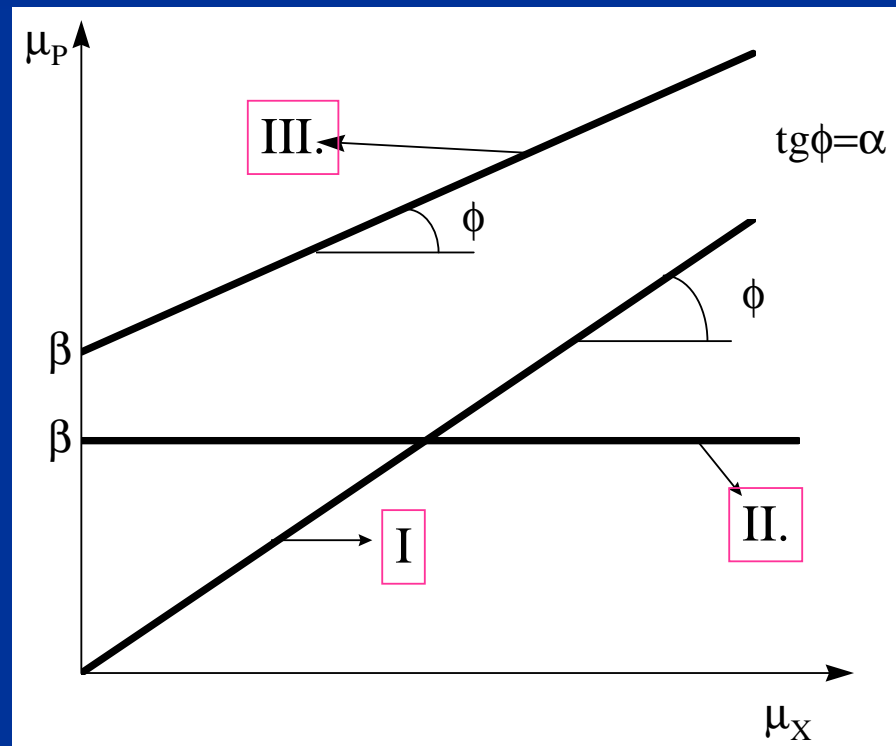


KINETICS OF PRODUCT FORMATION

LUEDEKING – PIRET MODEL

$$r_P = \frac{dP}{dt} = \alpha \frac{dx}{dt} + \beta x$$

$$\frac{1}{x} \frac{dP}{dt} = \mu_P = \alpha \mu_x + \beta$$



- I: $\alpha > 0$ és $\beta = 0$ **GROWTH ASSOC.**
- II: $\alpha = 0$ és $\beta > 0$ **NONGROWTH ASSOC**
- III: $\alpha > 0$ és $\beta > 0$ **MIXED TYPE**